

Grade 8 PI+ Yearlong Mathematics Map

Resources: Approved from Board of Education

Assessments: PARCC Assessments, Performance Series, District Benchmark Assessment

Common Core State Standards – Standards for Mathematical Practice:

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

| Conceptual Category | Domain | Cluster | Common Core Standard | Content | Skills | Academic Vocabulary |
|---------------------|--------|--|---|-----------------|--|---|
| G | CO | Experiment with transformations in the plane | G-CO.1 Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. | transformations | G-CO.1 - Define geometric terms based on undefined notions of point, line, distance along the line, and distance around a circular arc | Collinear, coplanar, postulate, skew, undefined terms, adjacent, bisector, complementary, congruent, opposite rays, plane, linear pair |
| G | CO | Experiment with transformations in the plane | G-CO.2 Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). | transformations | G-CO.2 - Model transformations visually in a plane | Rotational symmetry, prime notation, isometry, composition of transformations, angle of rotation, center of rotation, image, pre-image, glide reflection, line of reflection, rotation, translation |

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|---------------------|--------|--|---|-----------------|--|--|
| G | CO | Experiment with transformations in the plane | G-CO.2 Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). | transformations | G-CO.2 - Describe a transformation as a function | |
| G | CO | Experiment with transformations in the plane | G-CO.2 Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). | transformations | G-CO.2 - Compare isometries to non-isometries | |
| G | CO | Experiment with transformations in the plane | G-CO.3 Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. | transformations | G-CO.3 - Describe a polygon's rotational and/or reflectional symmetry | angle of rotation, center of rotation, image, pre-image, line of reflection, rotation, translation |
| G | CO | Experiment with transformations in the plane | G-CO.4 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. | transformations | G-CO.4 - Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments | isometry, composition of transformations, rotation, angle of rotation, center of rotation, image, pre-image, glide reflection, line of reflection, translation |

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|---------------------|--------|---|---|-----------------|---|--|
| G | CO | Experiment with transformations in the plane | G-CO.5 Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. | transformations | G-CO.5 - Draw a geometric figure after a transformation | composition of transformations, glide reflection, line of reflection, pre-image, image |
| G | CO | Experiment with transformations in the plane | G-CO.5 Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. | transformations | G-CO.5 - Identify a sequence of transformations that will carry given figure onto another | |
| G | CO | Understand congruence in terms of rigid motions | G-CO.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | congruence | G-CO.6 - Predict the effect of a given rigid motion transformation on a given figure | congruent, congruent figures, corresponding parts, rotation, reflection, translation |
| G | CO | Understand congruence in terms of rigid motions | G-CO.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. | congruence | G-CO.6 - Decide if two figures are congruent using the definition of congruence in terms of rigid motion | |
| G | CO | Understand congruence in terms of rigid motions | G-CO.7 Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent. | congruence | G-CO.7 - Justify that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angle are congruent, using the definition of congruence in terms of rigid motion | <i>corresponding parts, congruent, congruent figures</i> |
| G | CO | Understand congruence in terms of rigid motions | G-CO.8 Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. | congruence | G-CO.8 - Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. | <i>theorem, congruent, translation, reflection, rotation</i> |

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|---------------------|--------|------------------------------|--|---------------------------------------|---|--|
| G | CO | Prove geometric theorems | G-CO.9 Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints. | geometric theorems - lines and angles | G-CO.9 - Prove theorems about lines and angles | alternate exterior, alternate interior, consecutive, corresponding, transversal, <i>linear pair</i> , <i>supplementary</i> , <i>complementary</i> , <i>adjacent</i> , <i>bisector</i> , <i>vertical angles</i> |
| G | CO | Prove geometric theorems | G-CO.10 Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point. | geometric theorems - triangles | G-CO.10 - Prove theorems about triangles | theorem, midsegment, <i>interior angles</i> , <i>vertex angle</i> , <i>triangle sum theorem</i> |
| G | CO | Prove geometric theorems | G-CO.11 Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals. | geometric theorems - parallelograms | G-CO.11 - Prove theorems about parallelograms | <i>diagonal</i> , <i>congruent</i> , <i>convex</i> |
| G | CO | Make geometric constructions | G-CO.12 Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line. | Geometric Constructions | G-CO.12 - Create formal geometric constructions with a variety of tools and methods | <i>plane</i> |

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|---------------------|--------|--|--|--|---|---|
| G | CO | Make geometric constructions | G-CO.13 Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle. | Geometric Constructions | G-CO.13 - Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle | <i>interior angles</i> |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.1 Verify experimentally the properties of dilations given by a center and a scale factor: | similarity transformations - (Dilations) | G-SRT.1 - Verify experimentally the properties of dilations given by a center and a scale factor | <i>pre-image, image</i> |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.1a A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged. | similarity transformations - (Dilations) | G-SRT.1a - Verify experimentally the properties of dilations given by a center and a scale factor | <i>pre-image, image, transformation</i> |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.1b The dilation of a line segment is longer or shorter in the ratio given by the scale factor. | similarity transformations - (Dilations) | G-SRT.1b - Verify experimentally the properties of dilations given by a center and a scale factor | <i>pre-image, image, transformation</i> |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides. | Similarity of figures | G-SRT.2 - Decide if two figures are similar using the definition of similarity | <i>corresponding parts, interior angles, transformations</i> |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides. | Similarity in triangles | G-SRT.2 - Explain the meaning of similarity for triangles using similarity transformations | |
| G | SRT | Understand similarity in terms of similarity transformations | G-SRT.3 Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar. | Similarity in triangles | G-SRT.3 - Establish the AA criterion using properties of similarity transformations for two triangles | <i>transformations, corresponding parts, triangle sum theorem</i> |

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| G | SRT | Prove theorems involving similarity | G-SRT.4 Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity. | Similarity theorems in triangles. | G-SRT.4 - Prove similarity theorems about triangles | midsegment |
| G | SRT | Prove theorems involving similarity | G-SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures. | Applications of similarity | G-SRT.5 - Solve problems in geometric figures using triangle congruence and triangle similarity | theorems, <i>congruent figures, corresponding parts</i> |
| G | SRT | Prove theorems involving similarity | G-SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures. | Applications of similarity | G-SRT.5 - Prove relationships in geometric figures using triangle congruence and triangle similarity | |
| G | SRT | Define trigonometric ratios and solve problems involving right triangles | G-SRT.6 Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. | Similarity of right triangles | G-SRT.6 - Define trigonometric ratios using similarity for acute angles in right triangles | Sine, Cosine, Tangent, <i>Pythagorean Triples, corresponding parts</i> |
| G | SRT | Define trigonometric ratios and solve problems involving right triangles | G-SRT.7 Explain and use the relationship between the sine and cosine of complementary angles. | Right triangle trigonometry | G-SRT.7 - Explain and interpret the relationship between the sine and cosine of complementary angles | sine, cosine, <i>complementary,</i> |
| G | SRT | Define trigonometric ratios and solve problems involving right triangles | G-SRT.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems. ★ | Application of right triangle trigonometry | G-SRT.8 - Solve right triangles in applied problems using trigonometric ratios & the Pythagorean Theorem | sine, cosine, tangent, <i>Pythagorean Theorem</i> |
| G | SRT | Apply trigonometry to general triangles | G-SRT.9 (+) Derive the formula $A = \frac{1}{2} ab \sin(C)$ for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side. | Apply trigonometry to general triangles | G-SRT.9 (+) Derive the formula $A = \frac{1}{2} ab \sin(C)$ for the area of a triangle | |
| G | SRT | Apply trigonometry to general triangles | G-SRT.10 (+) Prove the Laws of Sines and Cosines and use them to solve problems. | Prove Laws of Sines and Cosines | G-SRT.10 - Prove the Law of Sines and the Law of Cosines | |
| G | SRT | Apply trigonometry to general triangles | G-SRT.10 (+) Prove the Laws of Sines and Cosines and use them to solve problems. | Apply trigonometry to general triangles | G-SRT.10 - Solve for side lengths and angle measures using the Laws of Sines and Cosines | |

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| G | SRT | Apply trigonometry to general triangles | G-SRT.11 (+) Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces). | Apply trigonometry to general triangles | G-SRT.11 - Apply Laws of Sines and Cosines in general triangles | |
| G | C | Understand and apply theorems about circles | G-C.1 Prove that all circles are similar. | Similarity of Circles | G-C.1 Prove that all circles are similar | Radians, Arc Measure, Arc Length, Central Angle, <i>congruent circles</i> |
| G | C | Understand and apply theorems about circles | G-C.2 Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle. | Circles - relationships of angles and segments | G-C.2 - Describe and apply relationships among inscribed angles, radii, and chords | Inscribed angle, central angle, circumscribed angle, chord, tangent line, external tangent, internal tangent |
| G | C | Understand and apply theorems about circles | G-C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. | Circles - construction | G-C.3 - Construct the inscribed and circumscribed circles of a triangle | |
| G | C | Understand and apply theorems about circles | G-C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle. | Circles - proofs of angle properties | G-C.3 - Prove properties of angles for a quadrilateral inscribed in a circle | |
| G | C | Understand and apply theorems about circles | G-C.4 (+) Construct a tangent line from a point outside a given circle to the circle. | Circles - construction | G-C.4 (+) - Construct a tangent line from a point outside a given circle to the circle | |
| G | C | Find arc lengths and areas of sectors of circles | G-C.5 Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector. | Circles - Arc Length and Radians | G-C.5 - Derive the proportionality of the arc length to the radius, and define the radian measure as the constant of proportionality | Radian, sector area, intercepted arc, congruent arcs, arc length, arc measure, congruent circles |

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| G | C | Find arc lengths and areas of sectors of circles | G-C.5 Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector. | Circles - Area of sector | G-C.5 - Derive the formula for area of a sector using similarity | |
| G | GPE | Translate between the geometric description and the equation for a conic section | G-GPE.1 Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation. | Equations of Circles | G-GPE.1 - Derive the equation of a circle of given center and radius using the Pythagorean Theorem | Standard Equation of a Circle, <i>Pythagorean Theorem</i> |
| G | GPE | Translate between the geometric description and the equation for a conic section | G-GPE.1 Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation. | Equations of Circles | G-GPE.1 - Complete the square to find the center and radius of a circle given by an equation | |
| G | GPE | Translate between the geometric description and the equation for a conic section | G-GPE.2 Derive the equation of a parabola given a focus and directrix. | Equation of Parabola | G-GPE.2 Derive the equation of a parabola given a focus and directrix | Focus, Directrix, <i>parabola</i> |
| G | GPE | Use coordinates to prove simple geometric theorems algebraically | G-GPE.4 Use coordinates to prove simple geometric theorems algebraically. For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point (1, $\sqrt{3}$) lies on the circle centered at the origin and containing the point (0, 2). | Coordinate Geometry | G-GPE.4 - Prove simple geometric theorems algebraically using coordinate geometry | <i>Distance Formula, Pythagorean Theorem</i> |
| G | GPE | Use coordinates to prove simple geometric theorems algebraically | G-GPE.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | Parallel & Perpendicular Lines | G-GPE.5 - Prove the slope criteria for parallel and perpendicular lines | slopes of parallel lines, slopes of perpendicular lines |

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| G | GPE | Use coordinates to prove simple geometric theorems algebraically | G-GPE.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point). | Equations of Parallel & Perpendicular Lines | G-GPE.5 - Solve geometric problems using slope criteria for parallel and perpendicular lines | |
| G | GPE | Use coordinates to prove simple geometric theorems algebraically | G-GPE.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio. | Coordinate Geometry | G-GPE.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio | <i>Pythagorean Theorem</i> |
| G | GPE | Use coordinates to prove simple geometric theorems algebraically | G-GPE.7 Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.★ | Coordinate Geometry - Perimeters & Area | G-GPE.7 - Compute perimeters of polygons and area of triangles and rectangles | <i>Distance Formula</i> |
| G | GMD | Explain volume formulas and use them to solve problems | G-GMD.1 Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments. | Formulas for area and volume | G-GMD.1 - Justify the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. | Radians, arc measure, arc length, sector area, <i>altitude</i> |
| G | GMD | Explain volume formulas and use them to solve problems | G-GMD.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.★ | Application of area & volume formulas | G-GMD.3 - Solve problems using formulas for cylinders, pyramids, cones, and spheres | <i>Right prism, prism, altitude</i> |
| G | GMD | Visualize relationships between two-dimensional and three-dimensional objects | G-GMD.4 Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects. | Cross sections of solids | G-GMD.4 - Identify the shapes of two-dimensional cross-sections of three-dimensional objects | <i>cross sections, rotations</i> |

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| G | GMD | Visualize relationships between two-dimensional and three-dimensional objects | G-GMD.4 Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects. | Solids from Revolutions | G-GMD.4 - Identify three-dimensional objects generated by rotations of two-dimensional objects | |
| G | MG | Apply geometric concepts in modeling situations | G-MG.1 Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).★ | Model object using geometric shapes | G-MG.1 - Describe real-world objects using geometric shapes, their measures, and their properties | <i>prism, regular polygon, cross section</i> |
| G | MG | Apply geometric concepts in modeling situations | G-MG.2 Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).★ | Model area and volume | G-MG.2 - Apply concepts of density based on area and volume in modeling situations | |
| G | MG | Apply geometric concepts in modeling situations | G-MG.3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).★ | Solve design problems | G-MG.3 - Apply geometric methods to solve design problems | Efficiency, apothem |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events (“or,” “and,” “not”). | Interpret data | S-CP.1 - Describe events as subsets of a sample space using categories of the outcomes | conditional probability, union, intersection, complement, sample space |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events (“or,” “and,” “not”). | Interpret data | S-CP.1 - Classify events as unions, intersections, or complements of other events | |

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|---------------------|--------|--|---|-------------------------|---|--|
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.2 Understand that two events A and B are independent if the probability of A and B occurring together is the product of their probabilities, and use this characterization to determine if they are independent. | Independent probability | S-CP.2 - Define independent events in terms of the product of their probabilities | independent events, dependent events |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.2 Understand that two events A and B are independent if the probability of A and B occurring together is the product of their probabilities, and use this characterization to determine if they are independent. | Independent probability | S-CP.2 - Determine if two events are independent | |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.3 Understand the conditional probability of A given B as $P(A \text{ and } B)/P(B)$, and interpret independence of A and B as saying that the conditional probability of A given B is the same as the probability of A, and the conditional probability of B given A is the same as the probability of B. | Conditional probability | S-CP.3 - Define conditional probability given two events | conditional probability, independent events, dependent events, union, intersection |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.3 Understand the conditional probability of A given B as $P(A \text{ and } B)/P(B)$, and interpret independence of A and B as saying that the conditional probability of A given B is the same as the probability of A, and the conditional probability of B given A is the same as the probability of B. | Conditional probability | S-CP.3 - Interpret the independence of two events using the language of conditional probability | |

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| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results. | Interpret data | S-CP.4 - Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified | independent events, dependent events, sample space |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results. | Independent & conditional probability | S-CP.4 - Decide if events are independent and approximate conditional probabilities using the two-way table as a sample space | |
| S | CP | Understand independence and conditional probability and use them to interpret data | S-CP.5 Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. For example, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer. | Conditional probability | S-CP.5 - Explain the concepts of conditional probability in independence in everyday language and everyday situations | conditional probability, independent events, dependent events, sample space, intersection |

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|---------------------|--------|---|---|-------------------------------------|---|---|
| S | CP | Use the rules of probability to compute probabilities of compound events in a uniform probability model | S-CP.6 Find the conditional probability of A given B as the fraction of B's outcomes that also belong to A, and interpret the answer in terms of the model. | Conditional probability | S-CP.6 - Compute and interpret the conditional probability of A given B | conditional probability, independent events, dependent events, sample space, intersection |
| S | CP | Use the rules of probability to compute probabilities of compound events in a uniform probability model | S-CP.7 Apply the Addition Rule, $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$, and interpret the answer in terms of the model. | Addition Rule for probability | S-CP.7 - Apply and interpret the Addition Rule | conditional probability, independent events, dependent events, sample space, intersection |
| S | CP | Use the rules of probability to compute probabilities of compound events in a uniform probability model | S-CP.8 (+) Apply the general Multiplication Rule in a uniform probability model, $P(A \text{ and } B) = P(A)P(B A) = P(B)P(A B)$, and interpret the answer in terms of the model. This is for an advanced course | Multiplication Rule for probability | S-CP.8 - Apply and interpret the general Multiplication Rule in a uniform probability model | conditional probability, independent events, dependent events, sample space, intersection |
| S | CP | Use the rules of probability to compute probabilities of compound events in a uniform probability model | S-CP.9 (+) Use permutations and combinations to compute probabilities of compound events and solve problems. | Compound events | S-CP.9 - Compute probabilities of compound events using permutations and combinations | Permutations, combinations, compound events, |

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| S | CP | Use the rules of probability to compute probabilities of compound events in a uniform probability model | S-CP.9 (+) Use permutations and combinations to compute probabilities of compound events and solve problems. | Applications of permutations and combinations | S-CP.9 - Solve problems using permutations and combinations | |
| S | MD | Use probability to evaluate outcomes of decisions | S-MD.6 (+) Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator). This is for an advanced course | Applications of probability | S-MD.6 - Make fair decisions using probability | |
| S | MD | Use probability to evaluate outcomes of decisions | S-MD.7 (+) Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game). This is for an advanced course | Evaluate outcomes using probability | S-MD.7 - Analyze decisions and strategies using probability concepts | |
| NEG | | | Explore Non-Euclidean vs Euclidean Geometry | | | Line segment, Circle, Parallel lines, Sphere, Great Circle, Arc of a Great Circle, Antipodal points (Pole Points, Small Triangle, Lune, Spherical, Hyperbolic |